## Multiview LSA: Representation Learning Via Generalized CCA

Pushpendre Rastogi<sup>1</sup>, Benjamin Van Durme<sup>1,2</sup>, Raman Arora<sup>1</sup>

<sup>1</sup>Center for Language and Speech Processing, JHU <sup>2</sup>Human Language Technology Center of Excellence

## Multiview LSA

- Represent datasets (linguistic or otherwise) as matrices, such that **each matrix is a view** of a word/phrase.
- Use Max-Var GCCA to create embeddings.
- Use **incremental SVD** so that the method can scale to handle millions of words/phrases and hundreds of views, where a view can be either a sparse or a dense matrix.
- Handle missing values instead of ignoring

## Max-Var GCCA

LSA is an application of PCA to a single termdocument cooccurrence matrix. CCA learns linear projections that are maximally correlated to each other from two views, Generalized CCA is a family of extensions of CCA to maximize correlation across *multi*ple views.

One variant of GCCA called MAX-VAR GCCA induces an auxilliary representation G that is maximally correlated to linear projections of the views in terms of sum of squared correlations [1, 2].

$$G = \operatorname{eig} \left( \sum_{j=1}^{J} P_j \right)$$
  
Where,  $P_j = X_j (X_j^{\top} X_j)^{-1} X_j^{\top}$ 

## Handling Missing Values

Sparse cooccurrence matrices contain plenty of missing values that cripple the performance of methods that rely on spectral decompositions. We address this sparsity by optimizing our representations only on the observed rows using a variant of MAX-Var GCCA presented by [3].

$$G = \operatorname{eig}\left( (\sum_{j} K_{j})^{-\frac{1}{2}} (\sum_{j=1}^{J} P_{j}) (\sum_{j} K_{j})^{-\frac{1}{2}} \right)$$
(1)

where  $[K_i]_{ii} = 1$  if row *i* of view *j* is observed and zero otherwise.

## **Further Information**

 Visit: www.cs.jhu.edu/~prastog3/mvlsa Email: pushpendre@jhu.edu

# baselines like Word2Vec and Glove [4, 5].

## Training Datasets

and Word2Vec

- 15 word history from Polyglot English Wikipedia Corpus

- Word alignment statistics from 6 Word Aligned bitext corpora (Arabic, Czech, German, Spanish, French, Chinese)

- Parent child cooccurrence events for 22 dependency relations from Annotated GigaWord

- Framenet Lexical Units augmented with PPDB paraphrases

- Morphological information from Catvar, Morpha, Morphg and Morphy - Embeddings generated by Glove

Test Set	Size	$\sigma^{0.9}_{0.05}$
MEN	3000	1.3
RW	2034	1.6
SCWS	2003	1.6
SIMLEX	999	2.3
WS	353	3.9
MTURK	287	4.3
WS-REL	252	4.6
WS-SEM	203	5.1
RG	65	9.2
MC	30	13.8
T-SYN	10675	0.68
T-SEM	8869	0.74
TOEFL	80	6.63

Table 1: Common test sets and associated MRDS values. MRDS=  $\sigma_{0.05}^{0.9}$  measures the minimum required difference between two algorithms for that difference to be significant with a pval of 0.05 assuming that the maximum correlation between the ratings produced by the competing algorithms is 0.9.





minimize: 
$$\sum_{j=1}^{J} \left\| W_{j} K_{j} (G - X_{j} U_{j}) \right\|_{F}^{2}$$
(2)  
subject to:  $G^{\top} G = I$   
 $[W_{j}]_{ii} = \left(\frac{w_{i}}{w_{\max}}\right)^{\frac{3}{4}}$  if  $w_{i} < w_{\max}$  else 1,  
and  $w_{i} = \sum_{k} [X_{j}]_{ik}.$